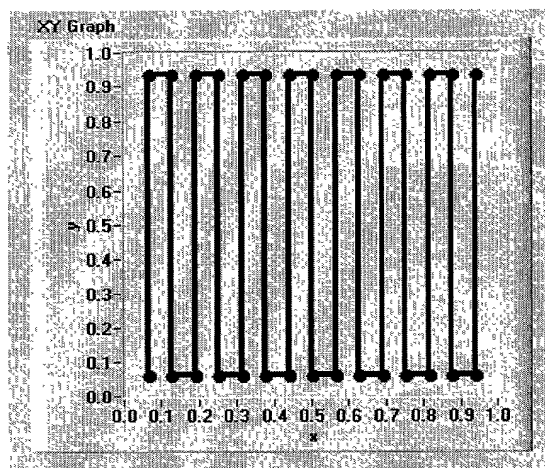


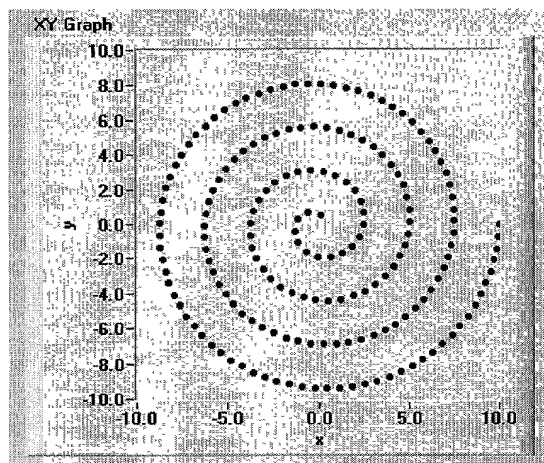
Approximated Peano Curve. The space-filling process has not been completed.

Figure 1A (Prior Art)



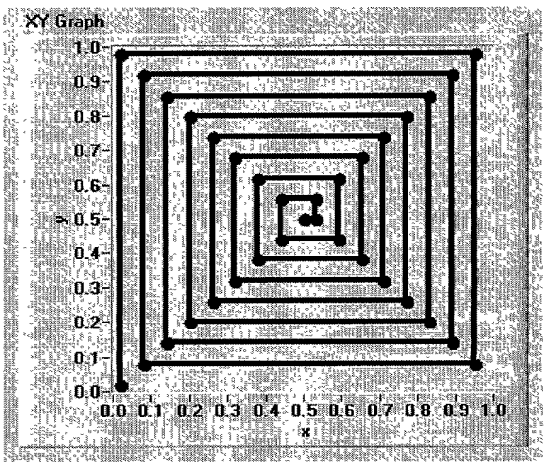
Boustrophedon Path

Figure 1B (Prior Art)



Archimedes Spiral defined by equally distributed points

Figure 1C (Prior Art)



Spiral-like line-based scanning

Figure 1D (Prior Art)

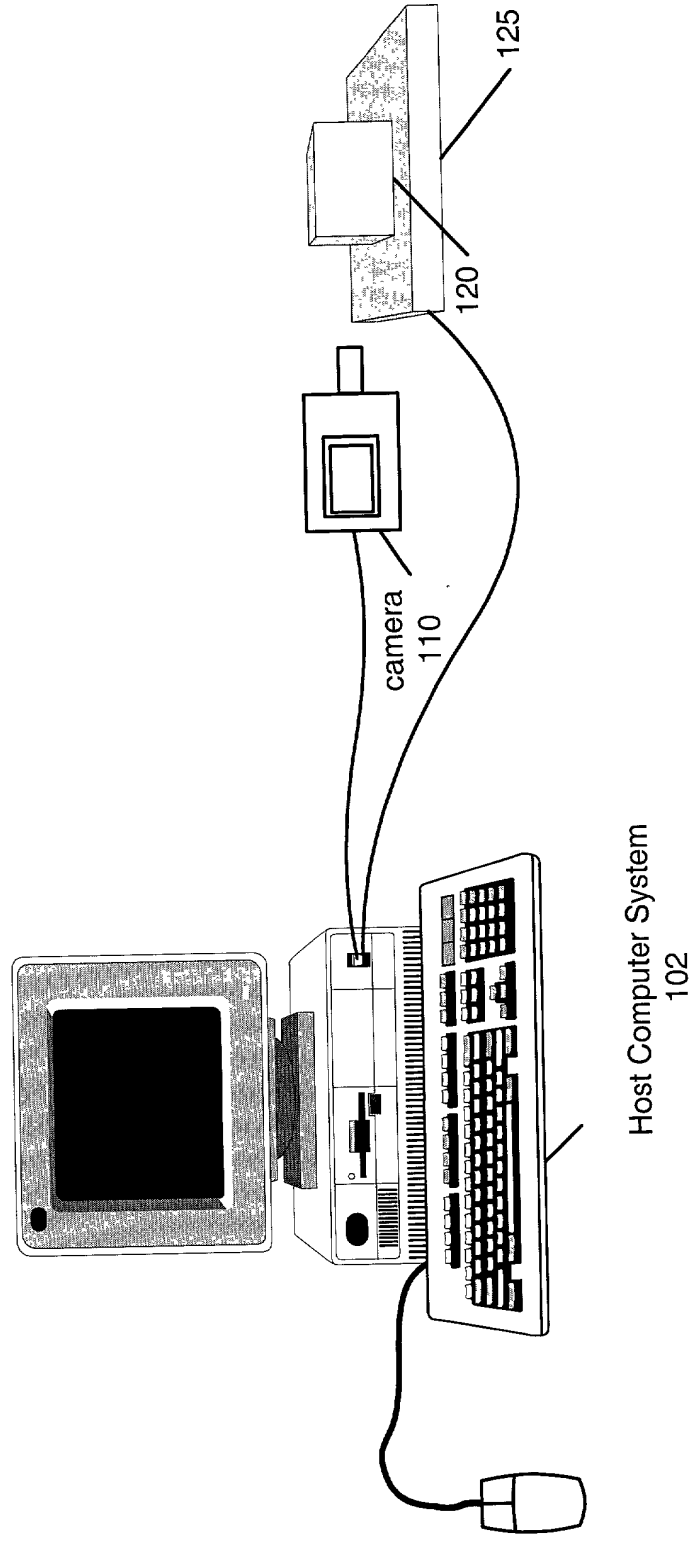


Figure 2A

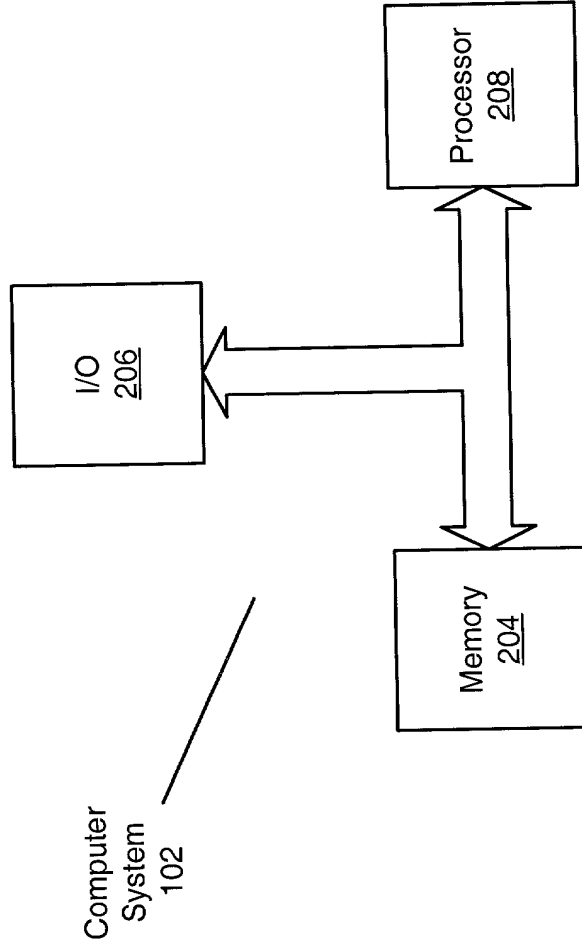


Figure 2B

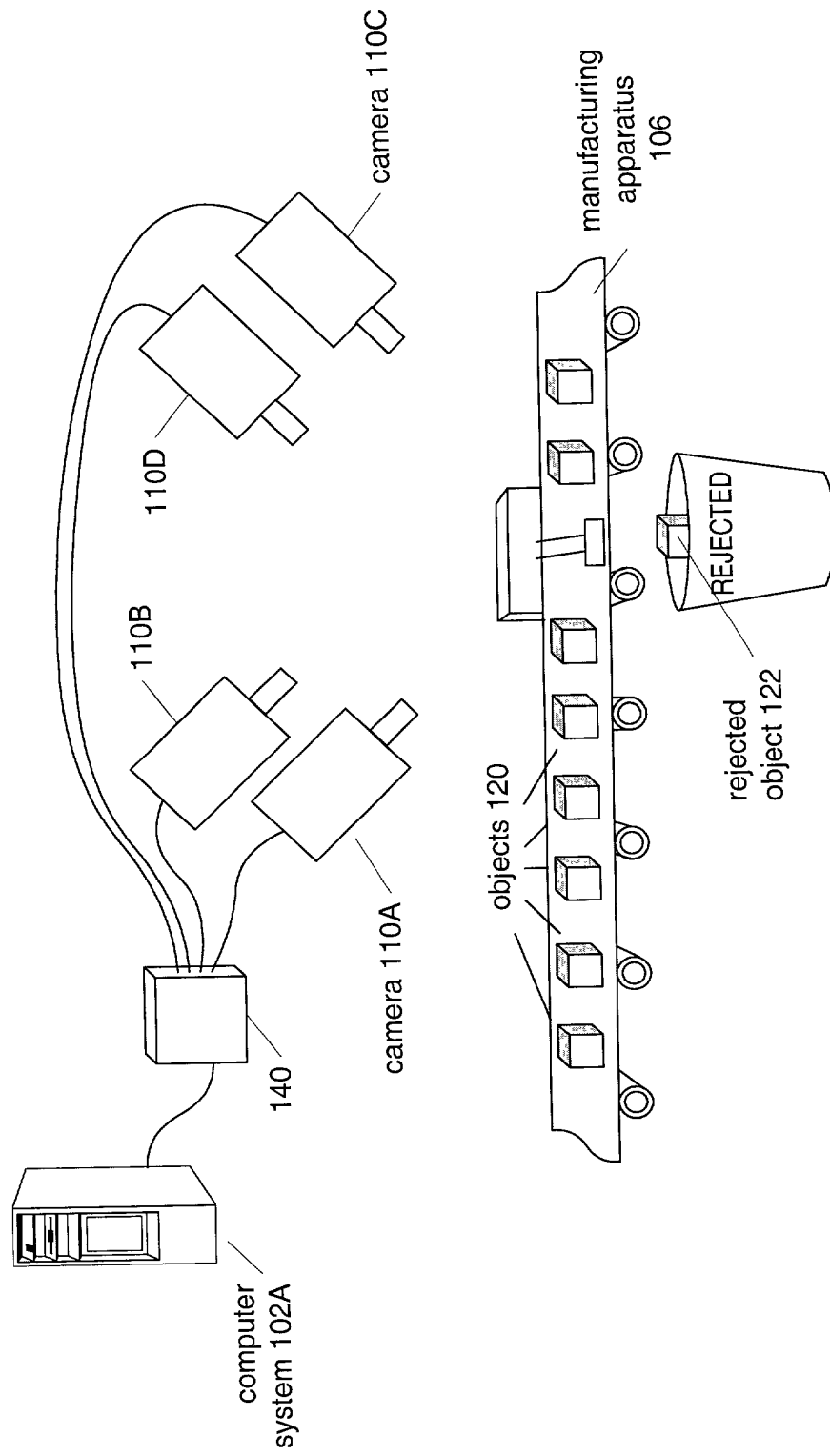


Figure 3A

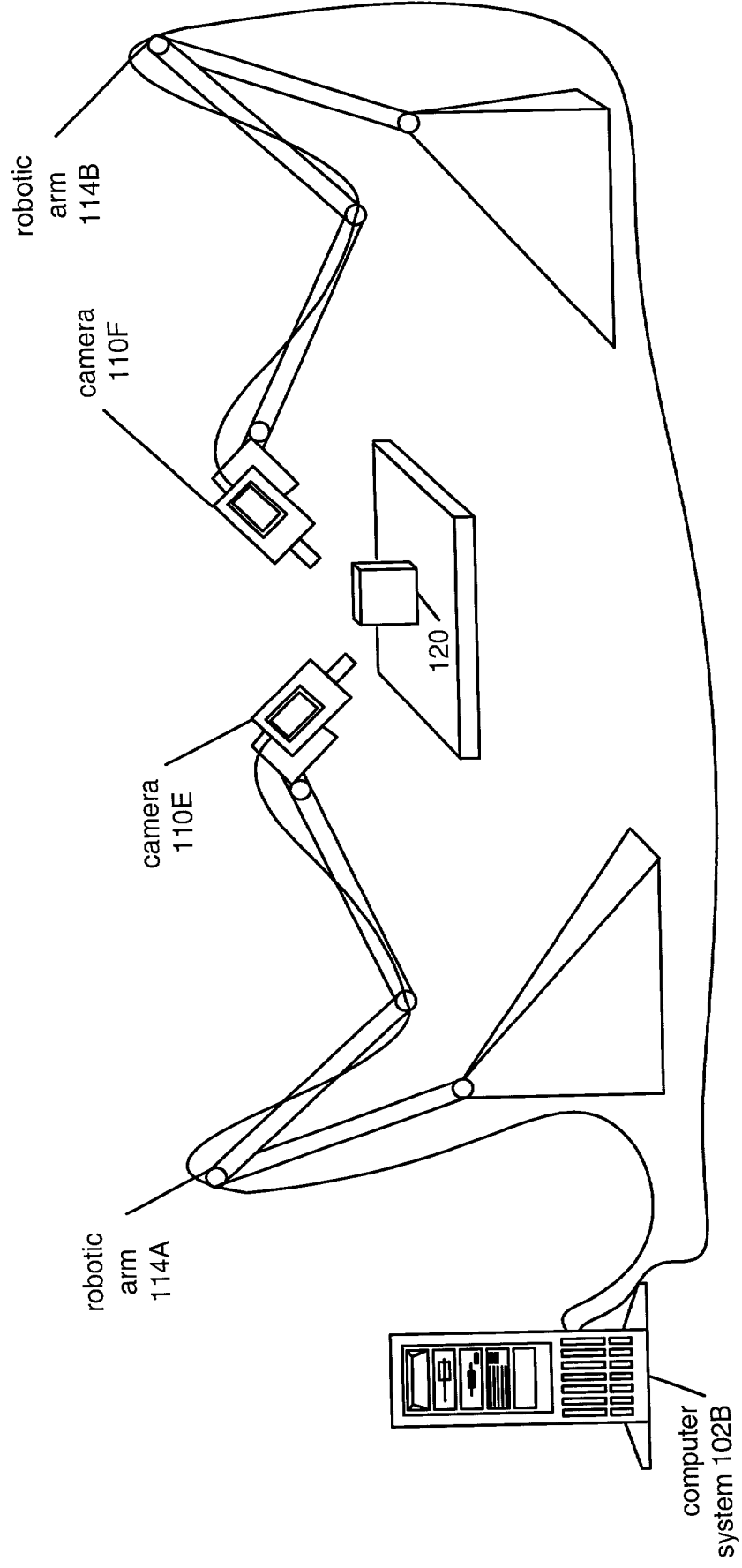


Figure 3B

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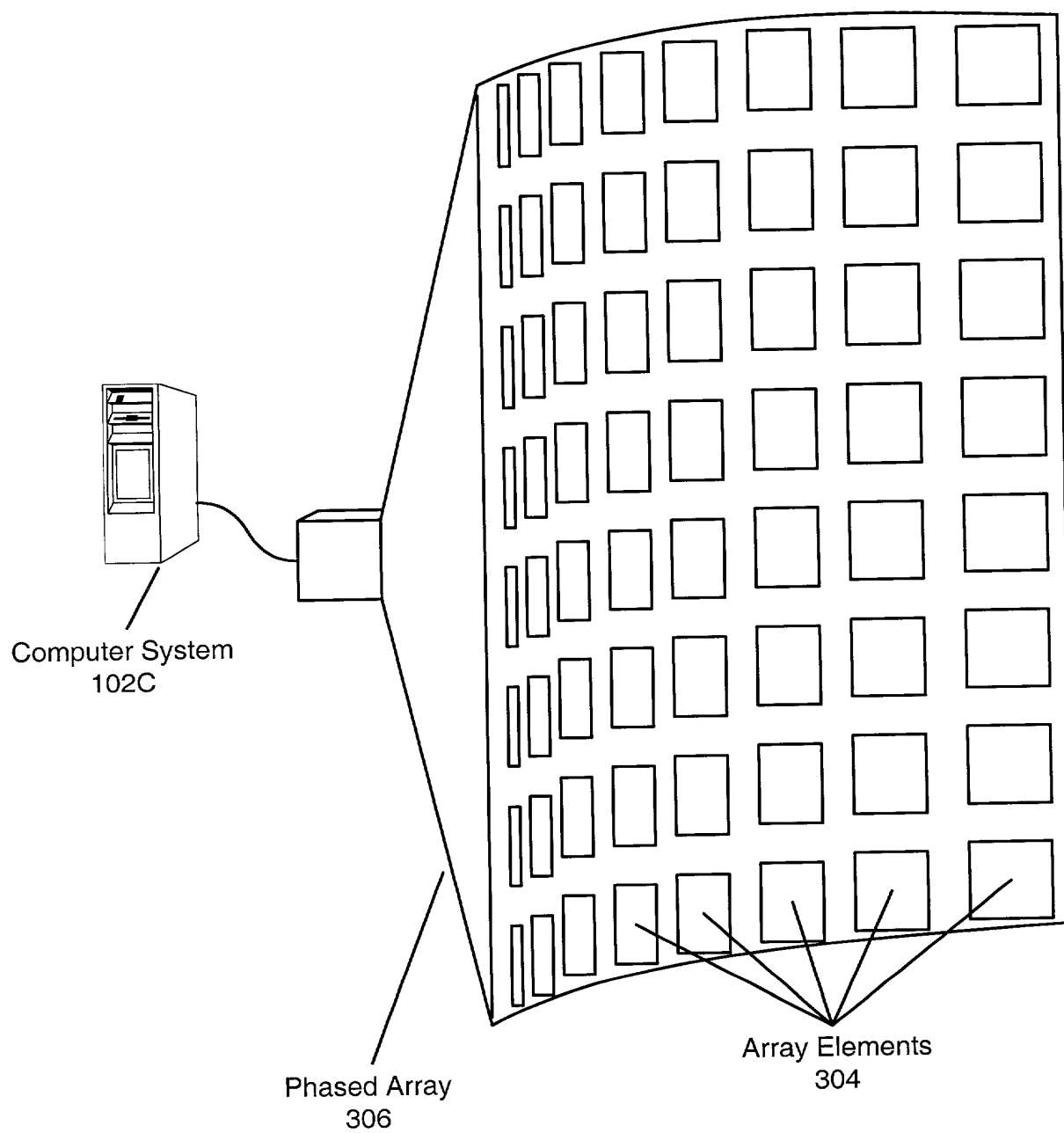
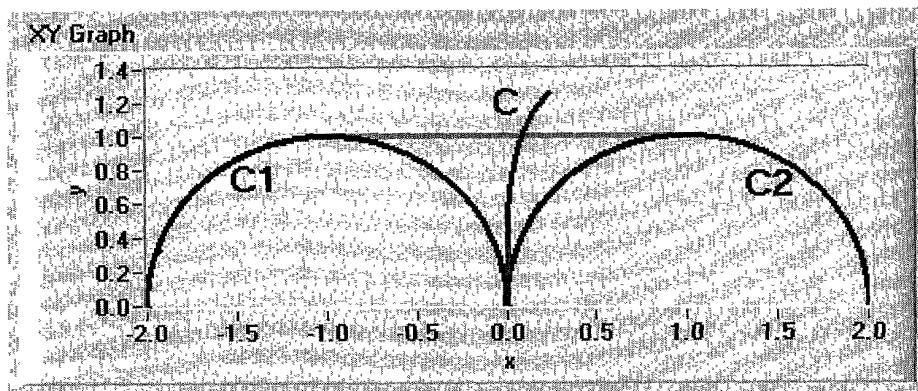


Figure 3C

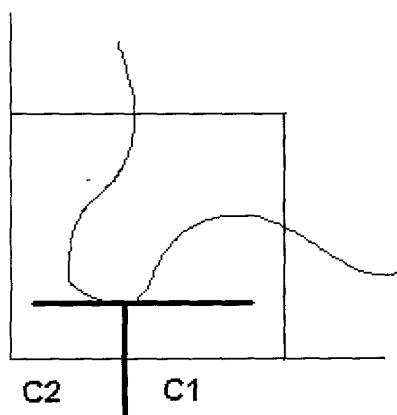


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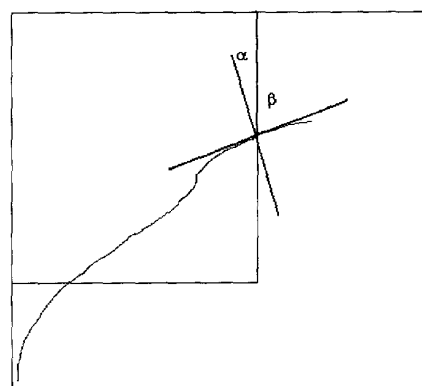
The situation of Lemma 1

Figure 4A



Case (A)

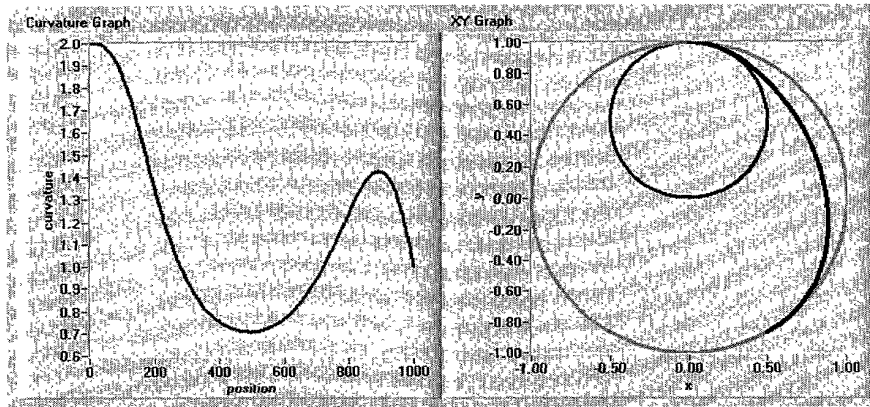
Figure 4B



Case (B)

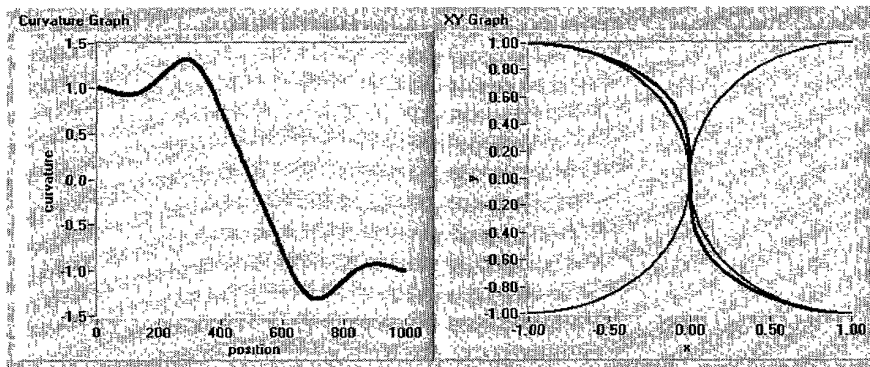
Figure 4C





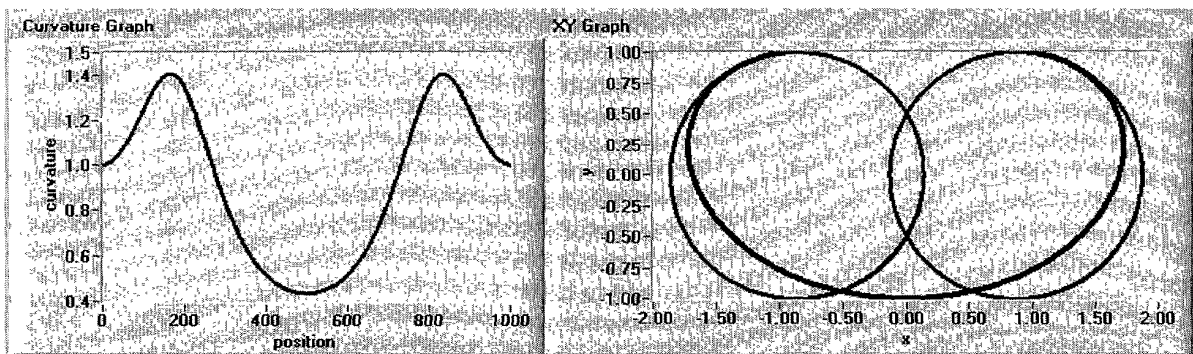
Smooth transition between two circles of different radii.

Figure 4D



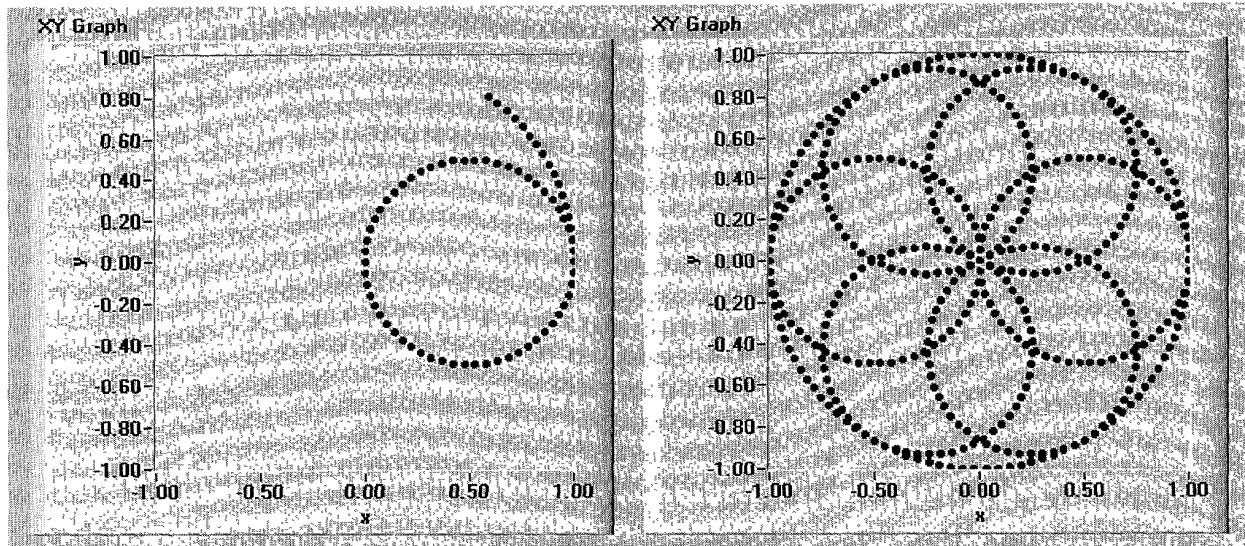
Smooth transition between two circles of same radius.

Figure 4E



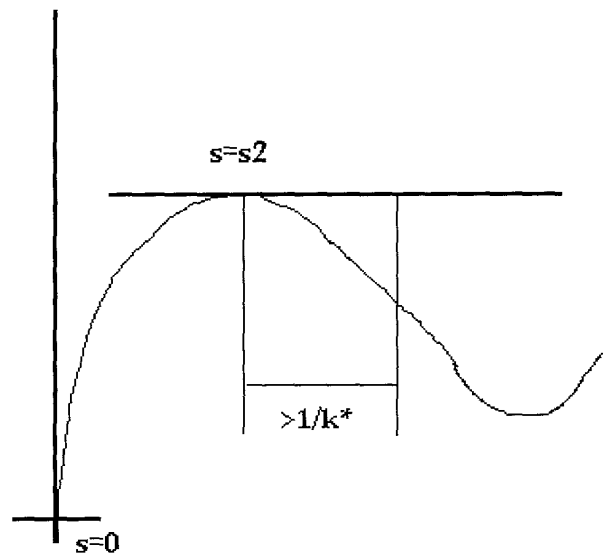
Transition between two unit circles of radius 1. The distance between the circles is  $\sqrt{3}$

Figure 4F



Beginning (left) and completion (right) of a scanning scheme where the curvature is below a certain value

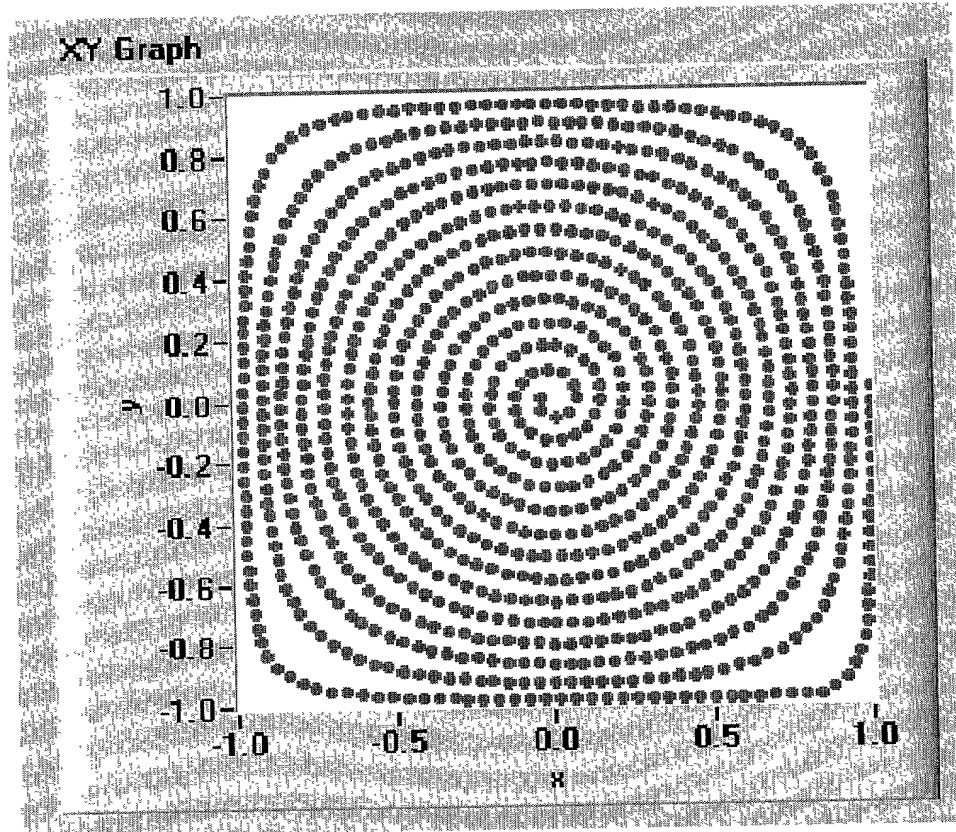
Figure 5A



Construction of  $s_2$  and the subsequent part of the curve

Figure 5B

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Conformal Spiral.

Figure 6

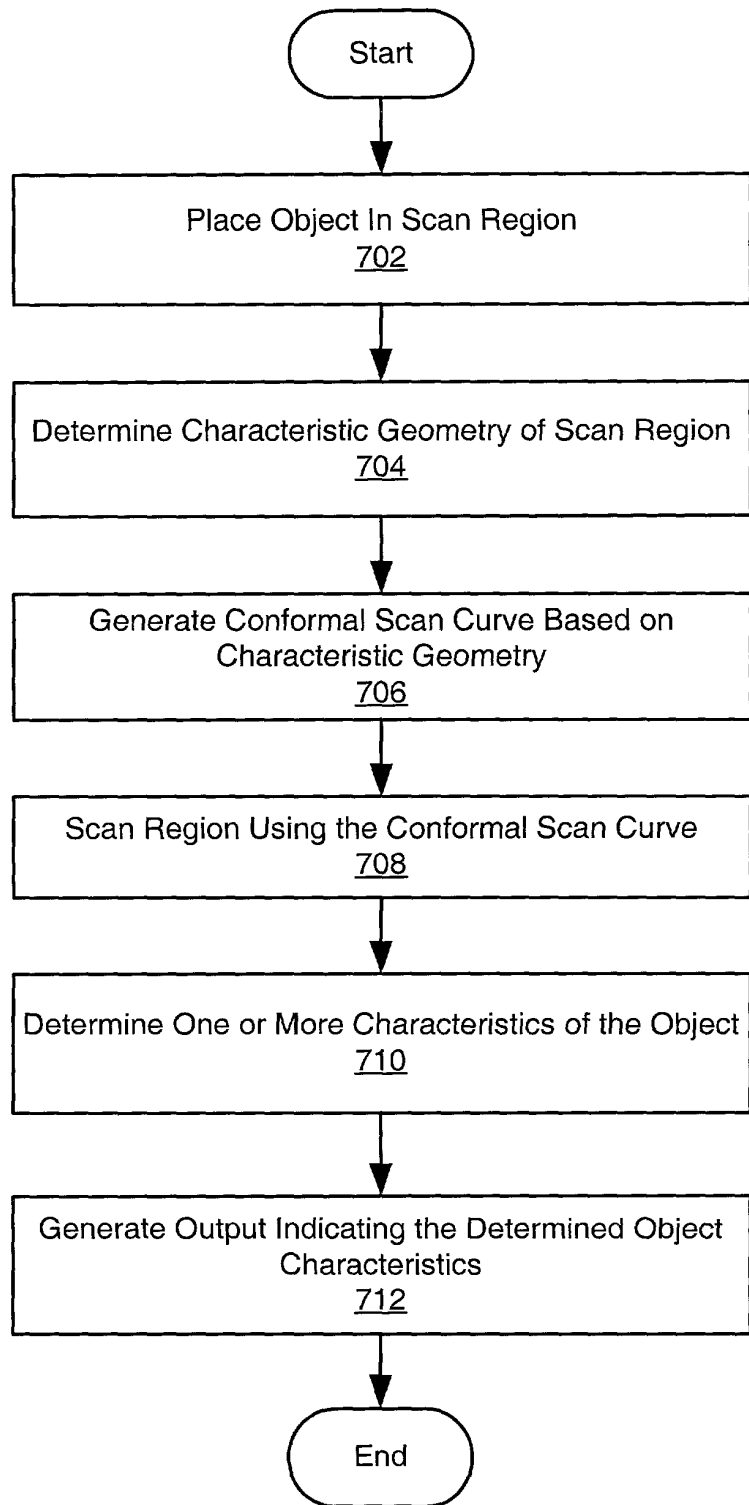
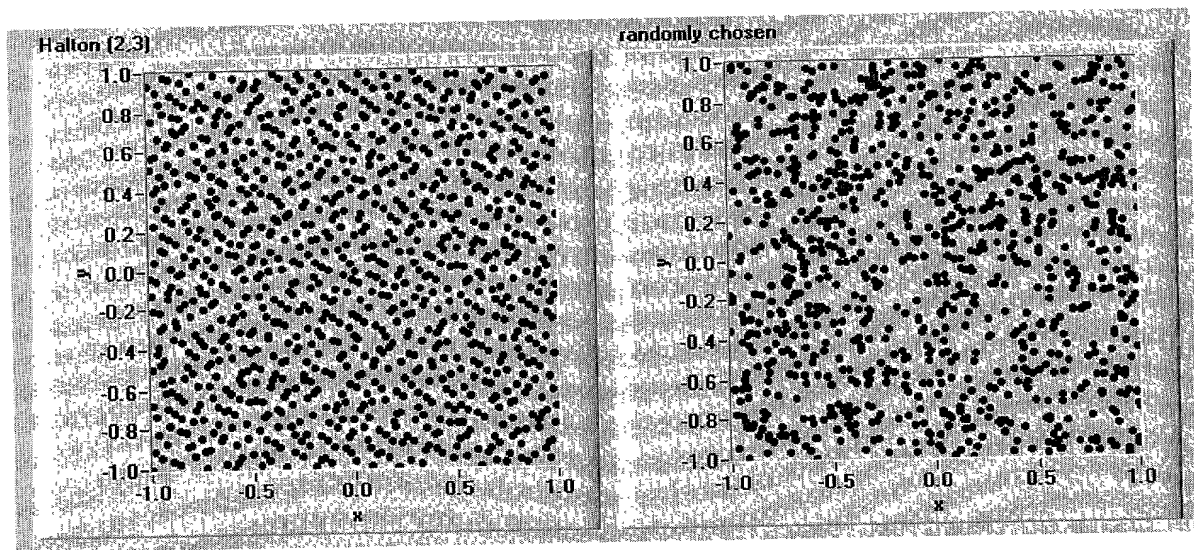
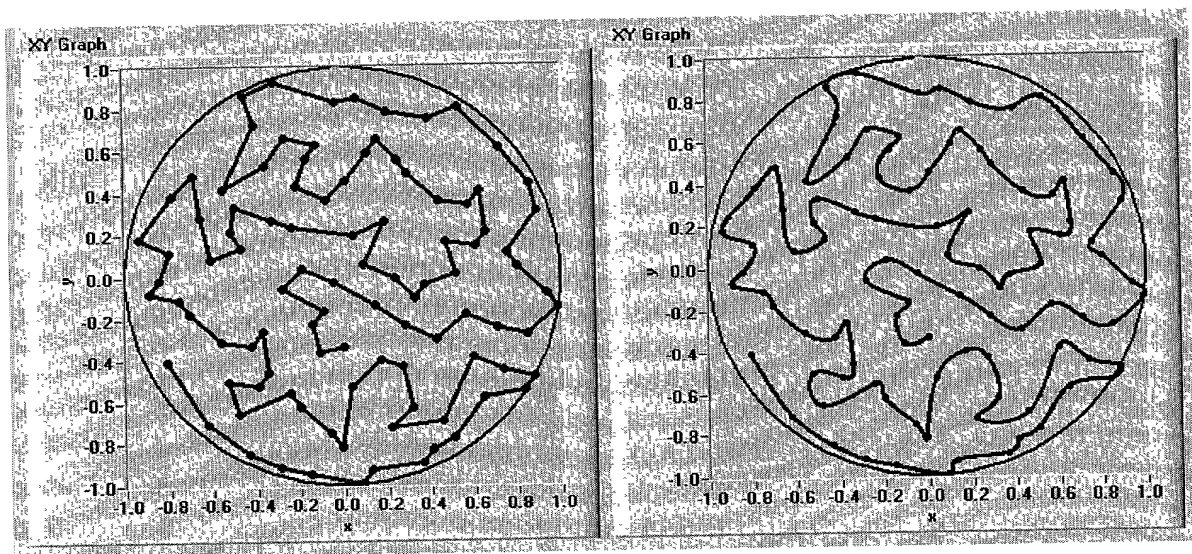


Figure 07



The first 1000 Halton points (left) and randomly chosen points (right)

Figure 8A



Original solution (left) and splined version (right).

Figure 8B

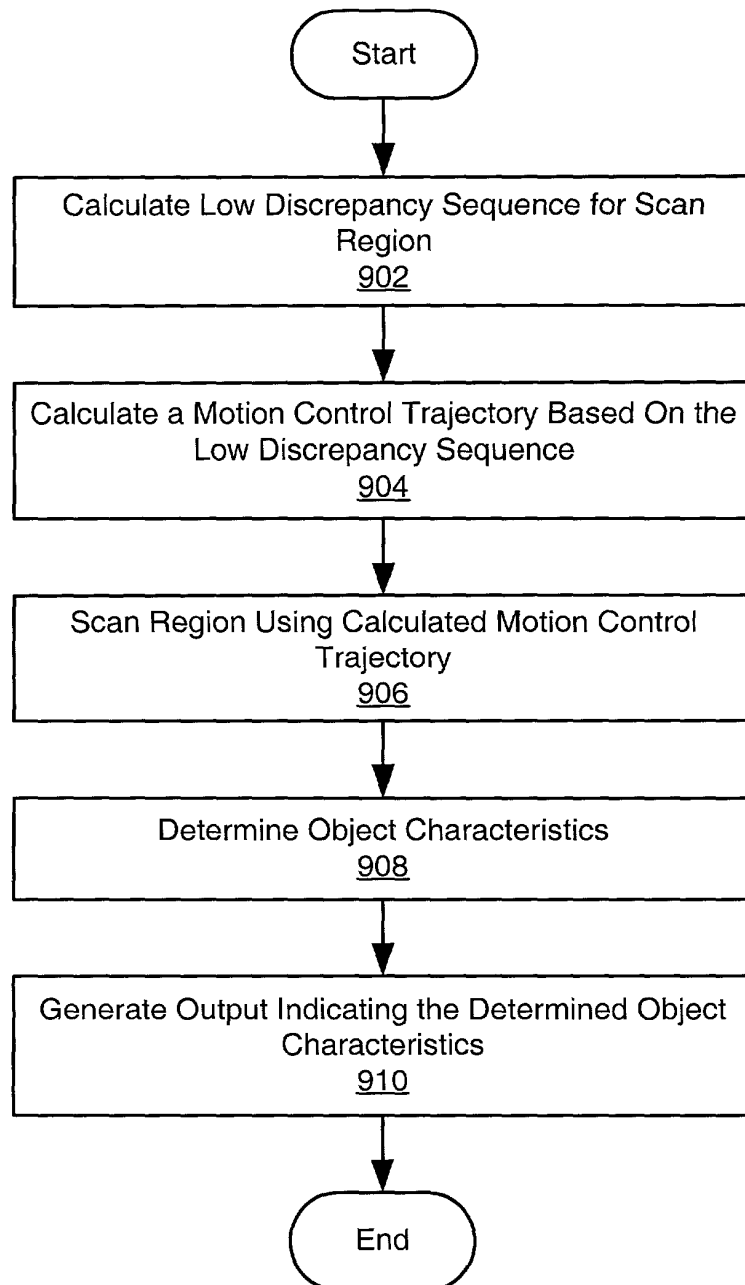
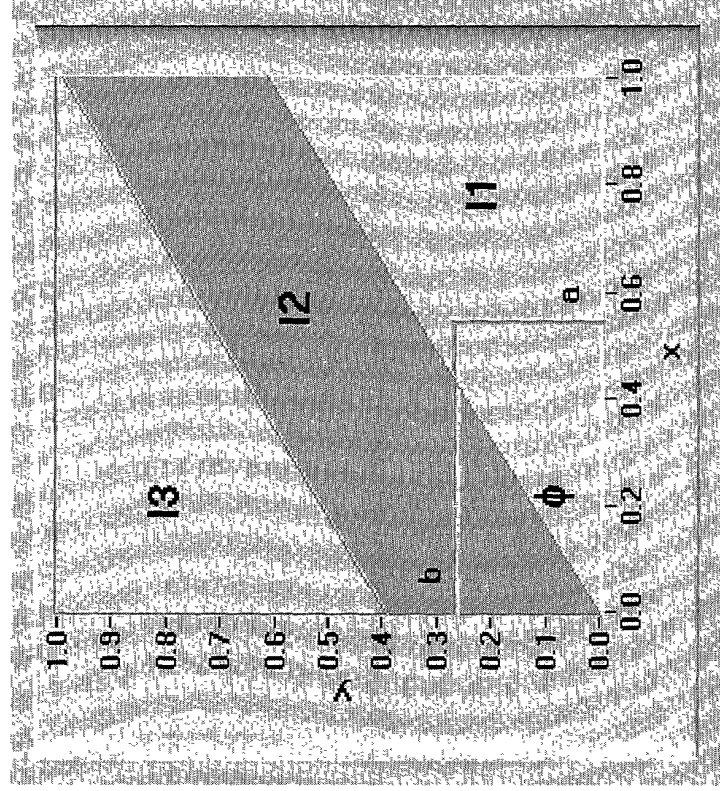


Figure 9



Definition of  $I_1$ ,  $I_2$ , and  $I_3$

Figure 10



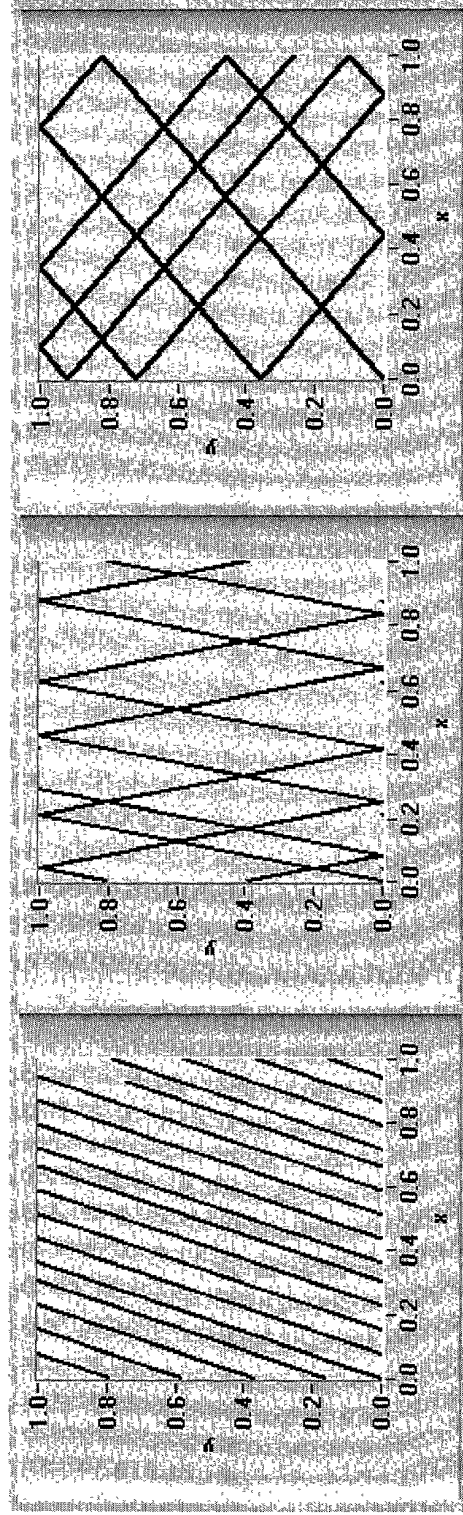


Figure 11A

Figure 11B

Figure 11C



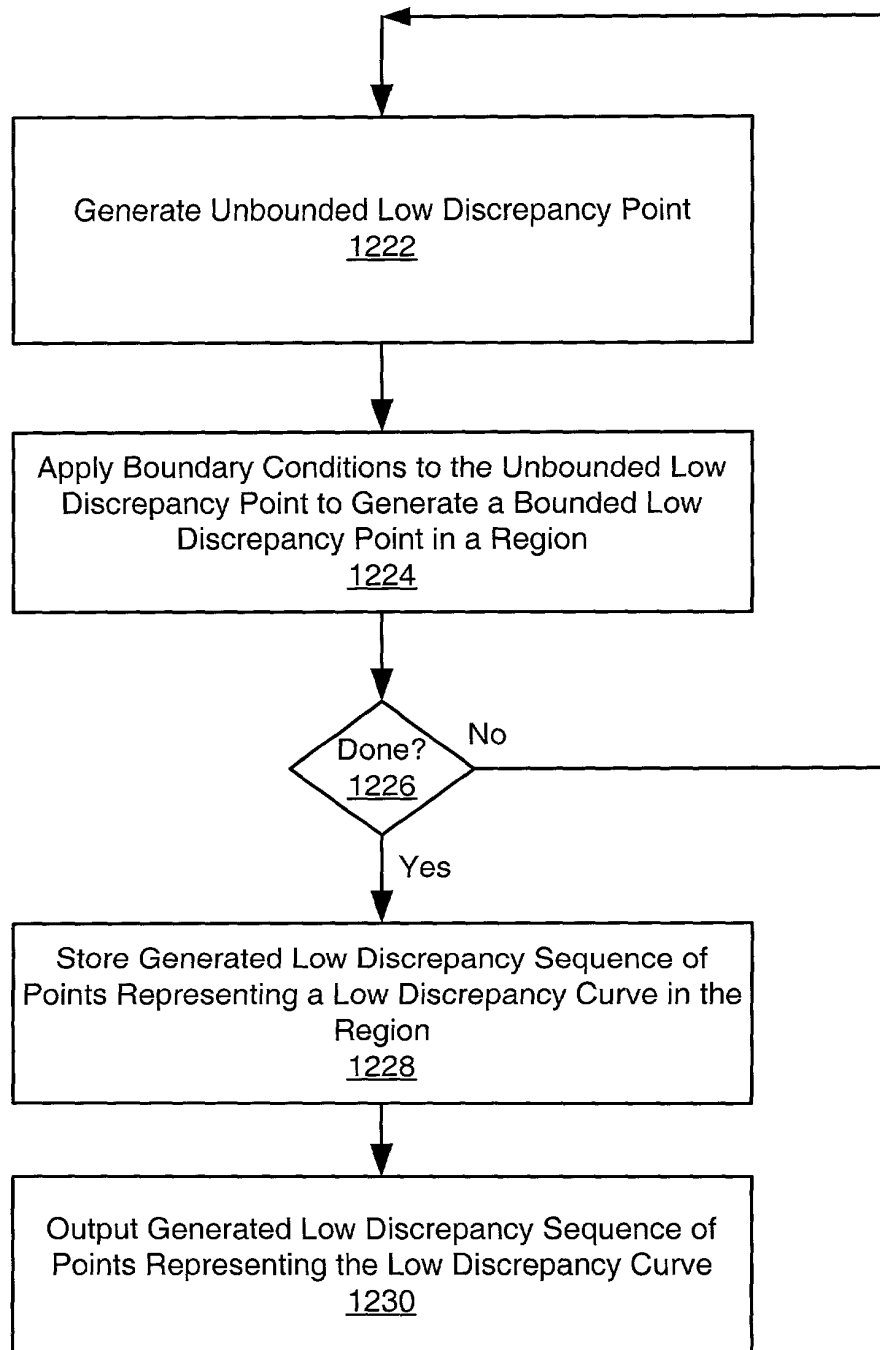


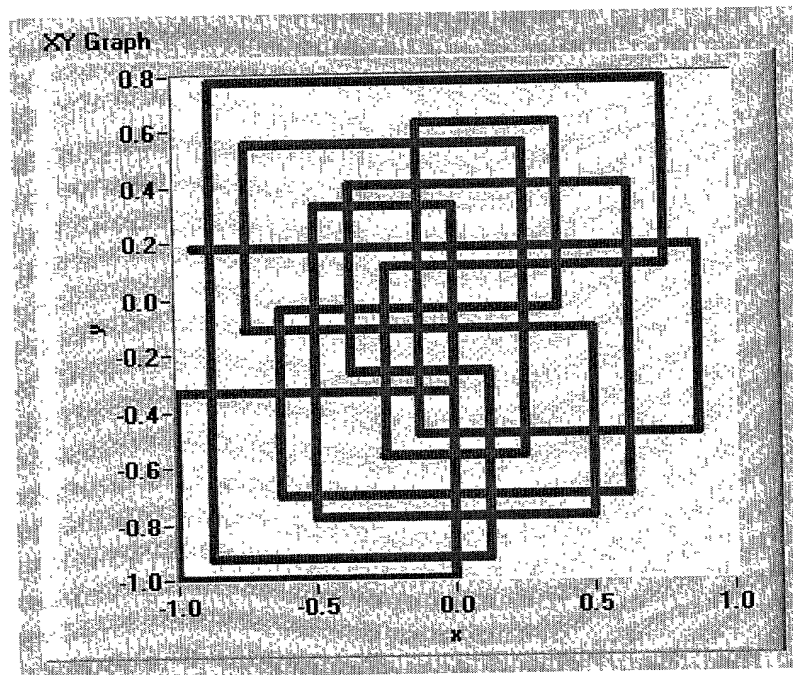
Figure 12A

```

graph TD
    1202[Select a Pair of Irrational Numbers (alpha1,alpha2) such that the Sequence  $\{(n \cdot \alpha_1) \bmod 1\}, \{(n \cdot \alpha_2) \bmod 1\}$  for all Natural Numbers n is a LDS in the Unit Square.  
1202] --> 1204[Select a Length, L, and a Step Rate, epsilon, of the LD Curve in the Unit Square  
1204]
    1204 --> 1206[Initialize Current Length, l, to Zero, and Initialize Current Position (x,y), (e.g., to (0,0))  
1206]
    1206 --> 1208[Increment x and y and Apply Boundary Conditions at Borders of Unit Square (e.g., Toroidal, Reflectance, or Both), Generating a Low Discrepancy Sequence Point  $(x_n, y_n)$   
1208]
    1208 --> 1210{Is l < L?  
1210}
    1210 -- Yes --> 1212[Output Generated Low Discrepancy Sequence of Points Representing the Low Discrepancy Curve  
1212]
    1210 -- No --> 1208
  
```

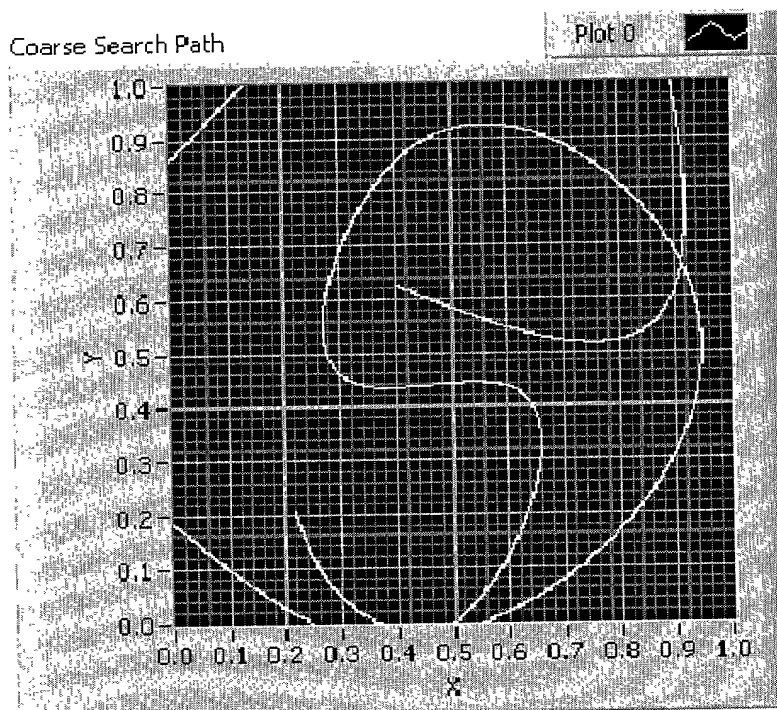
Figure 12B

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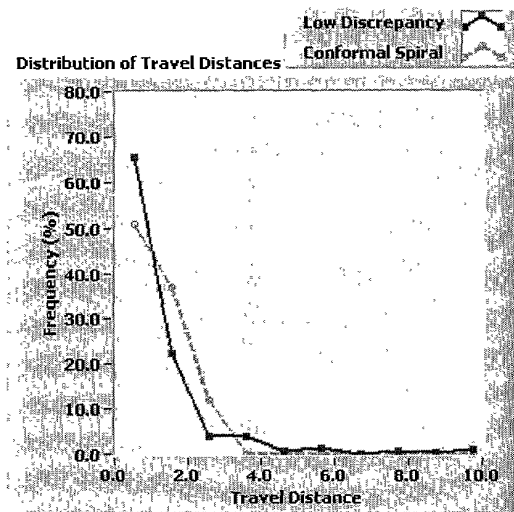
Beginning of a Low Discrepancy Curve based on a specific Halton Sequence in 2d

Figure 13A



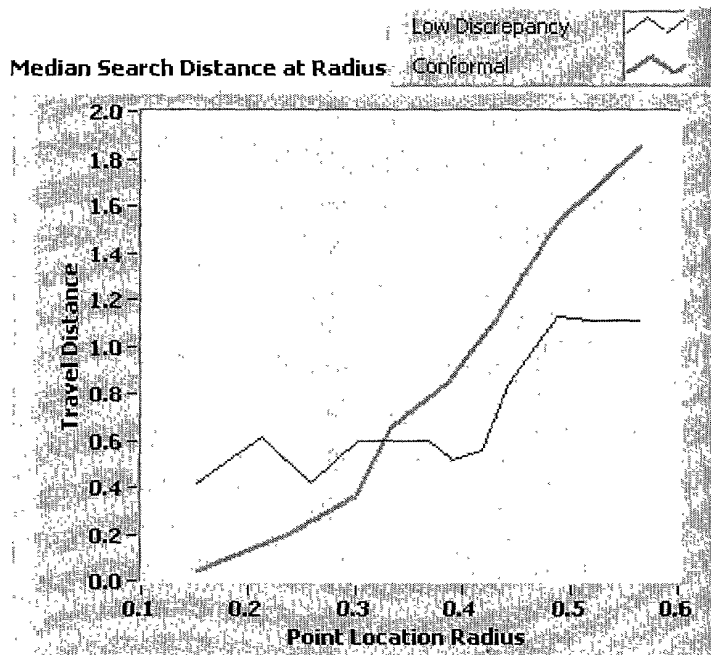
Splined Low Discrepancy Curve coarse search

Figure 13B



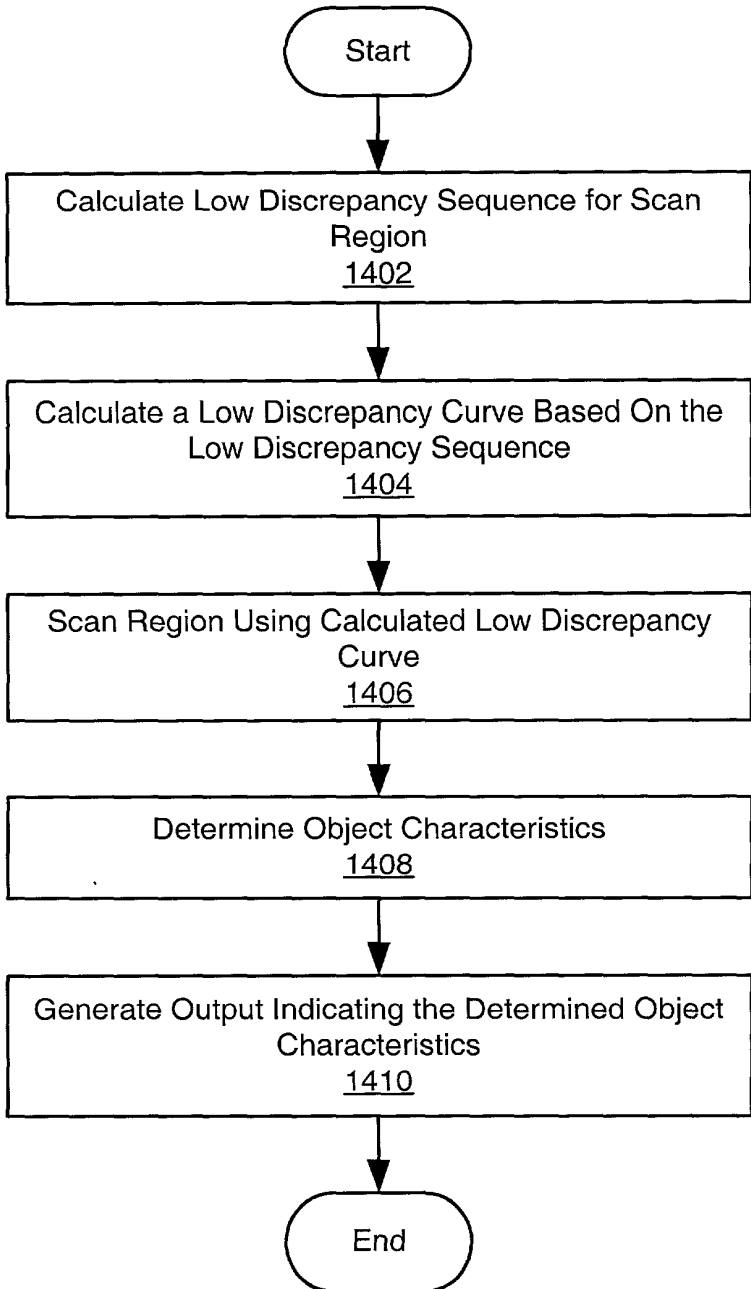
Comparison of Conformal Spiral and Low Discrepancy Searching

Figure 13C

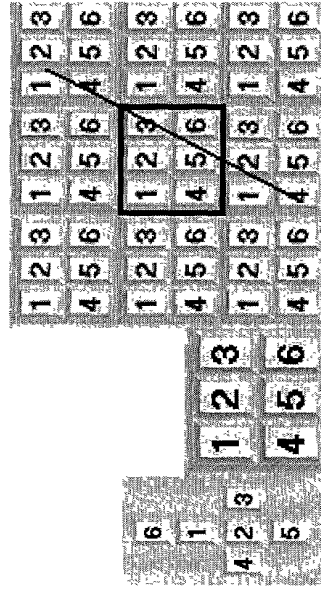


Comparison of Travel Distance for Low Discrepancy Search and Conformal Spiral Search

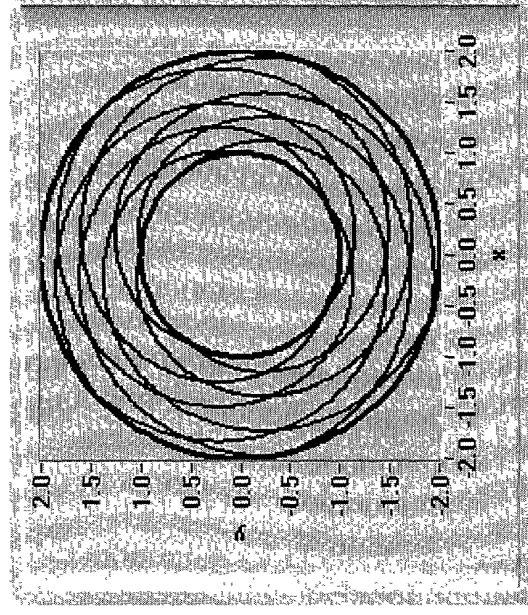
Figure 13D



### Figure 14



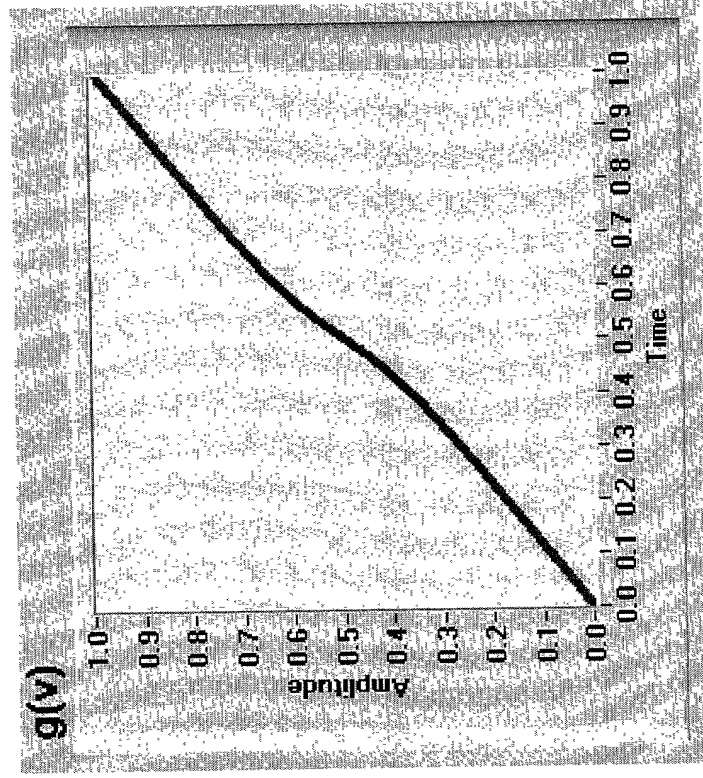
Tiling of the plane and relation to the surface of the unit cube



Low-discrepancy curve in a ring

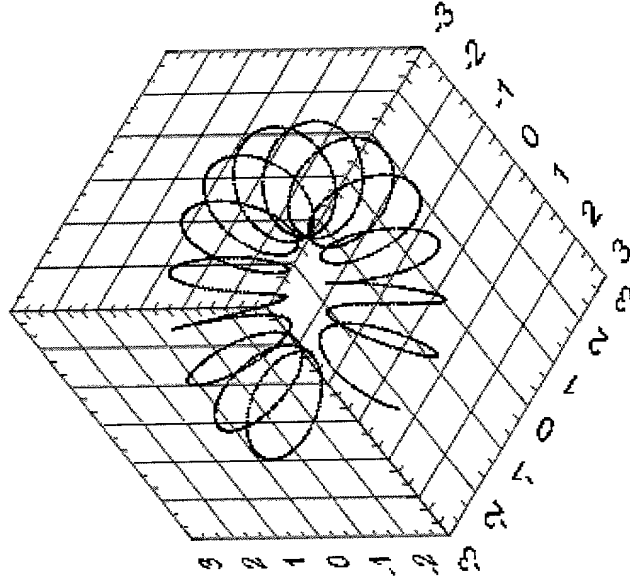
Figure 15A

Figure 15B



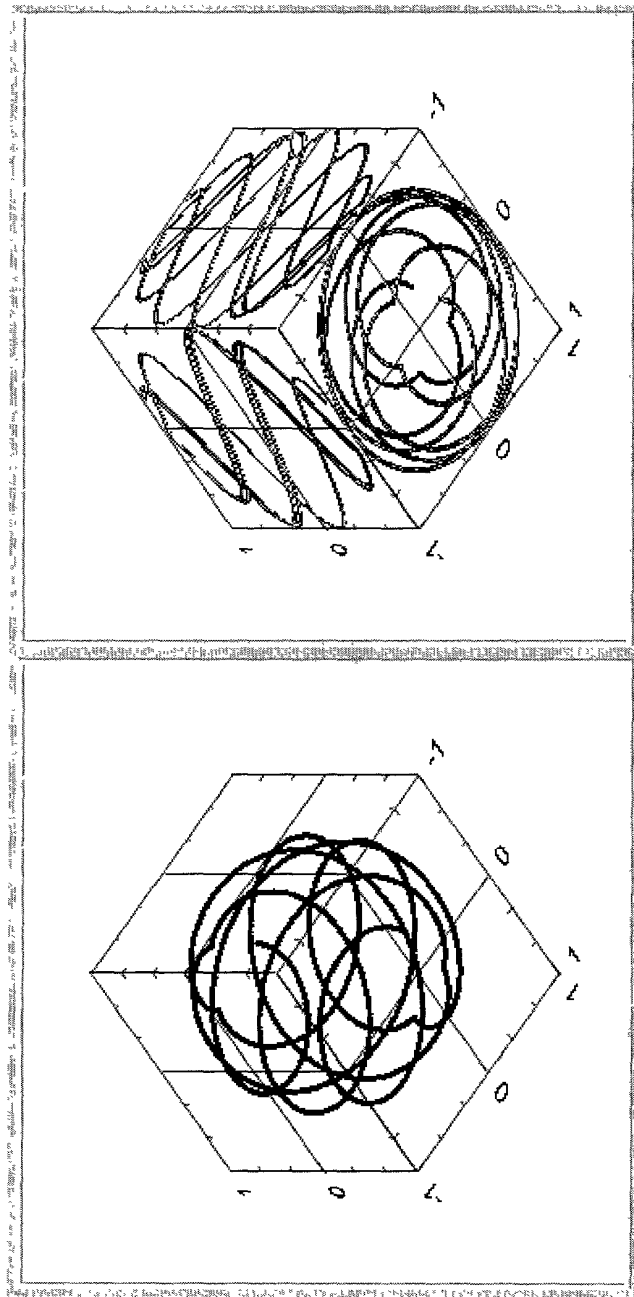
Low Discrepancy Preserving Mapping Function

Figure 15C



Low-discrepancy curve filling the surface of a torus

Figure 15D



Low-discrepancy curve on a sphere  
(left) and projections (right)

Figure 16



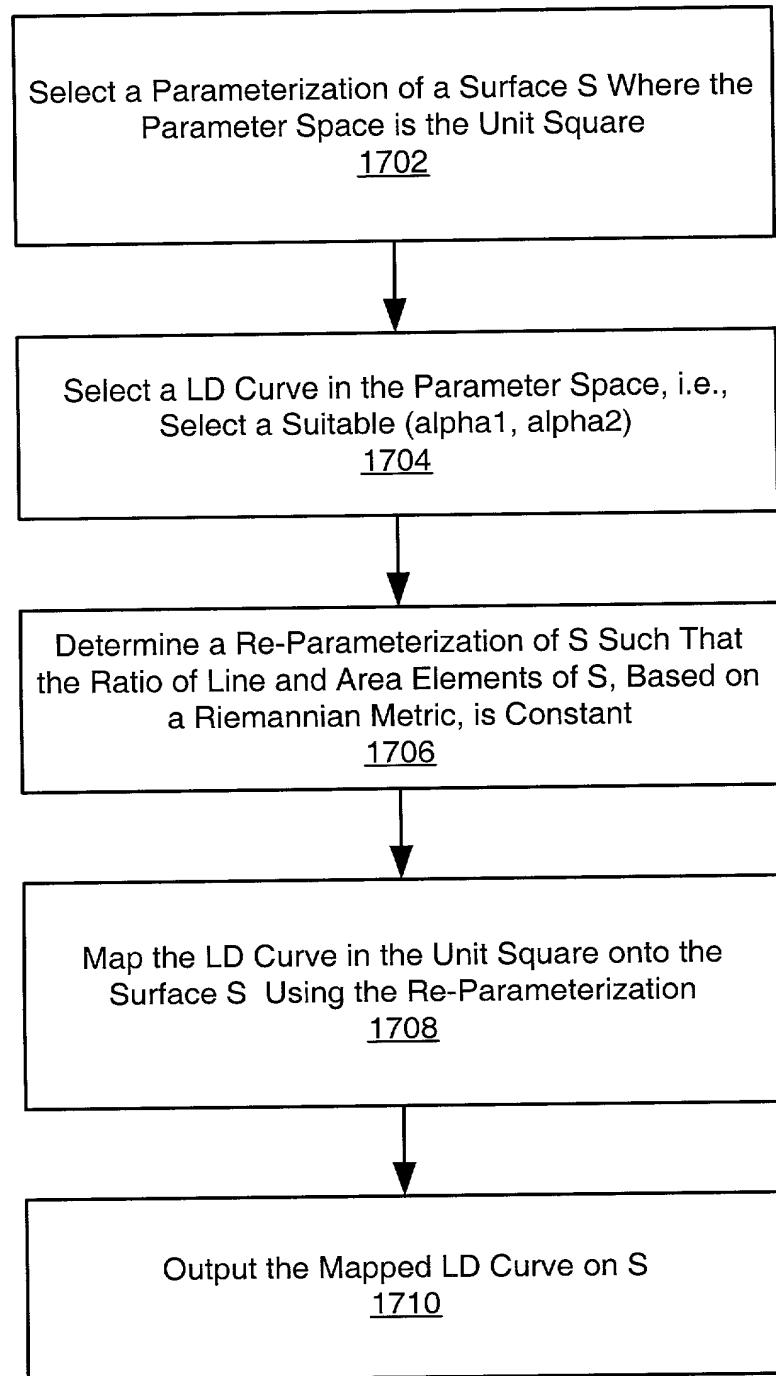
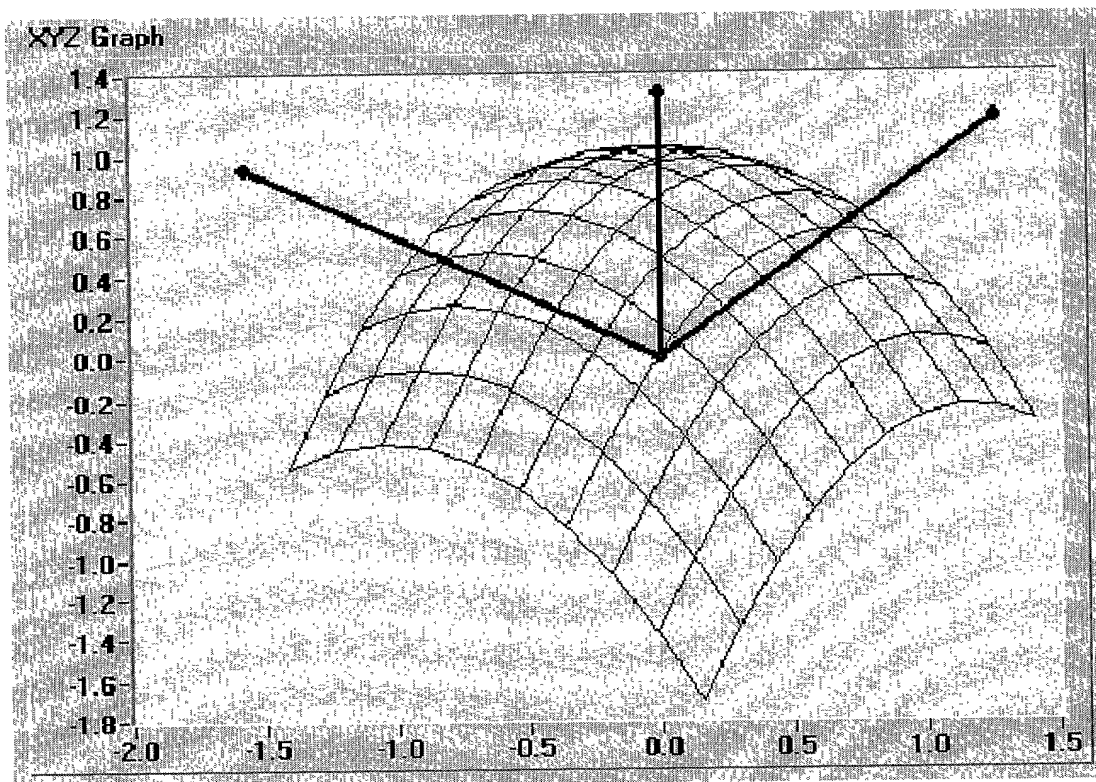


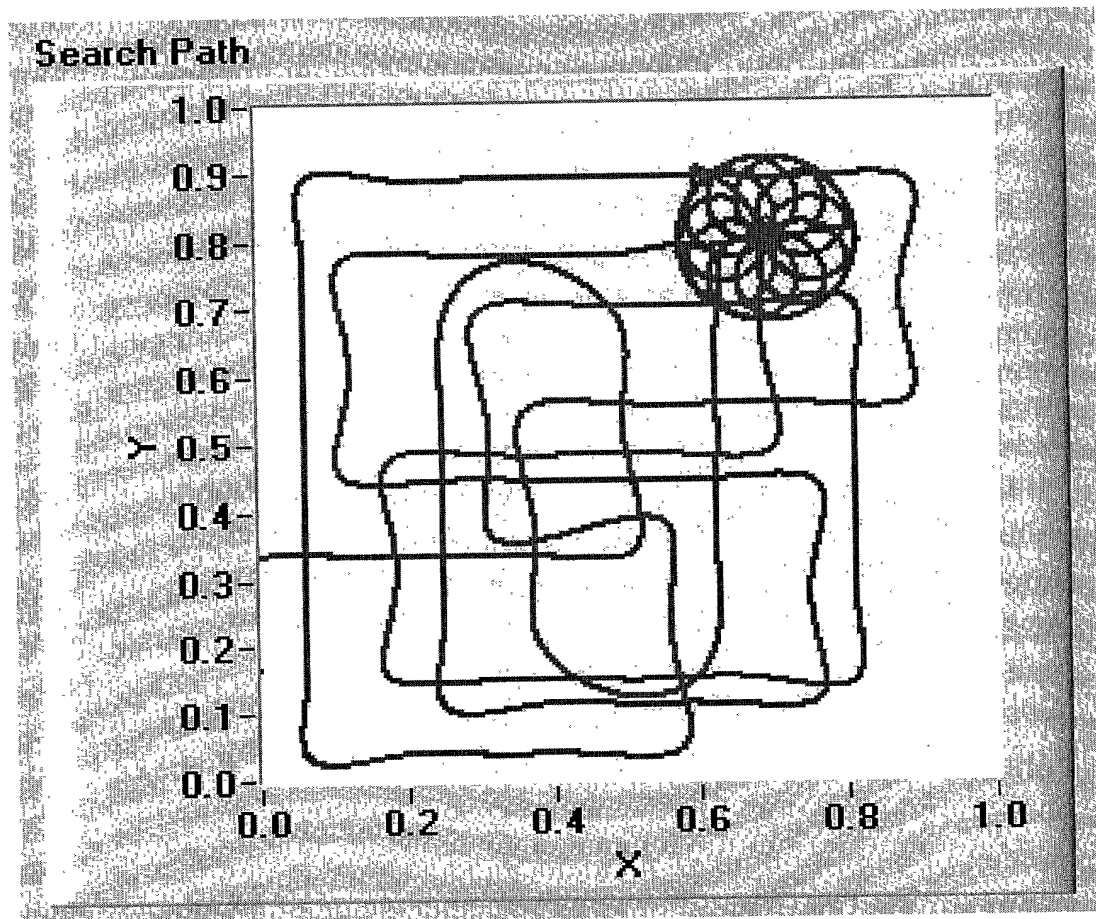
Figure 17



Surfaces can be scanned efficiently when the term low discrepancy sequence/ curve can be generalized, e.g. based on metrics on the surface.

Figure 18

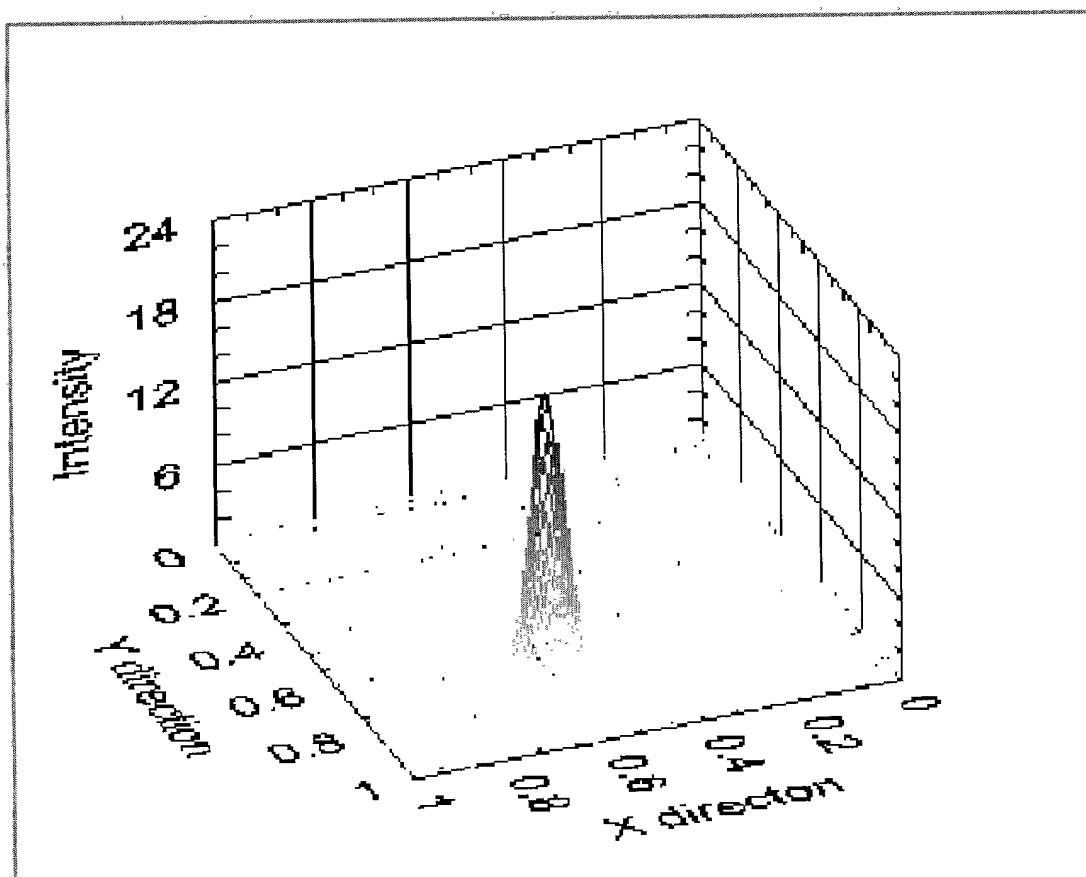
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Splined Low Discrepancy Curve coarse search with refined final approach

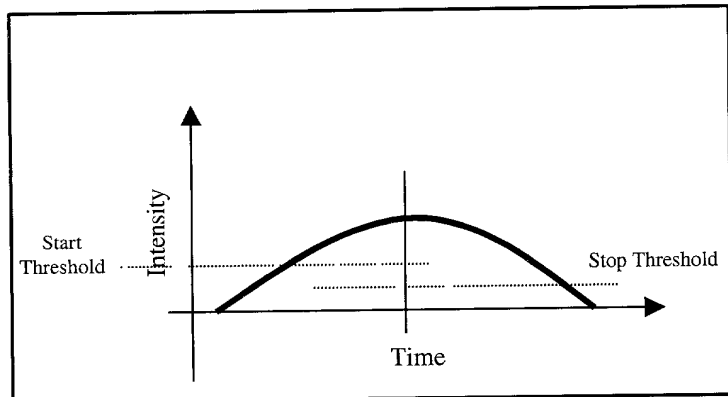
Figure 19

# Intensity Field Distribution in Search Area

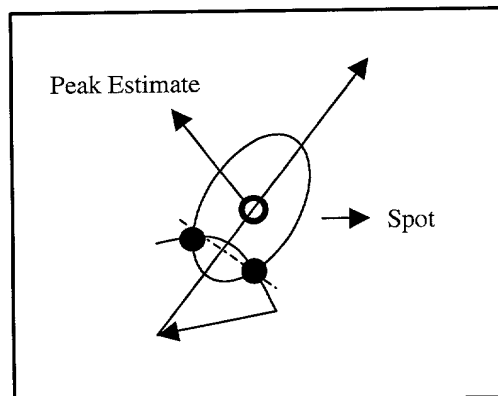


Beam intensity distribution in search area

Figure 20



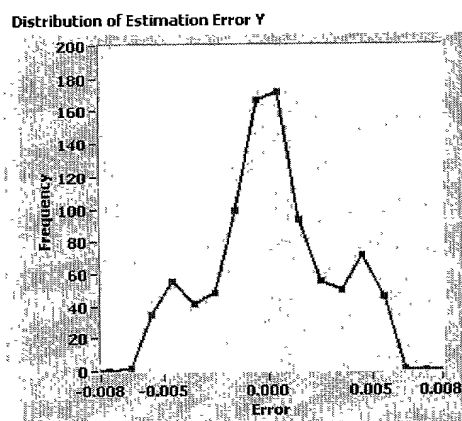
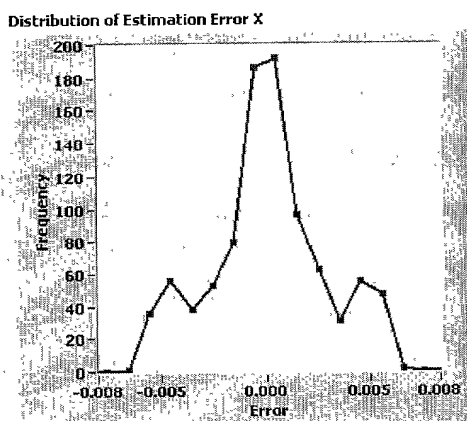
Location of the Peak



Initial Final Approach Move

Figure 21A

Figure 21B



Error distribution of the estimated peak X coordinate error (left) and Y coordinate error (right)

Figure 21C

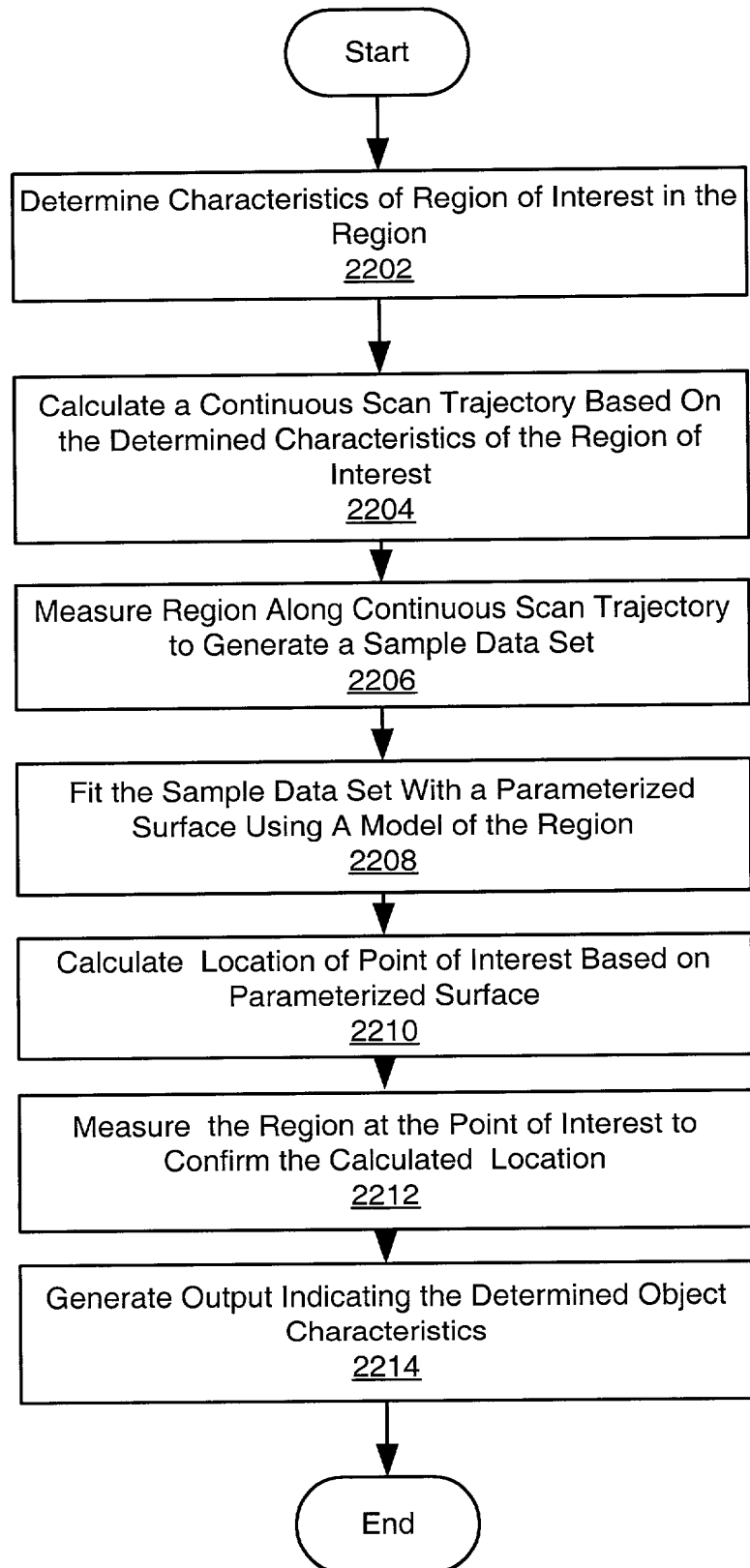


Figure 22

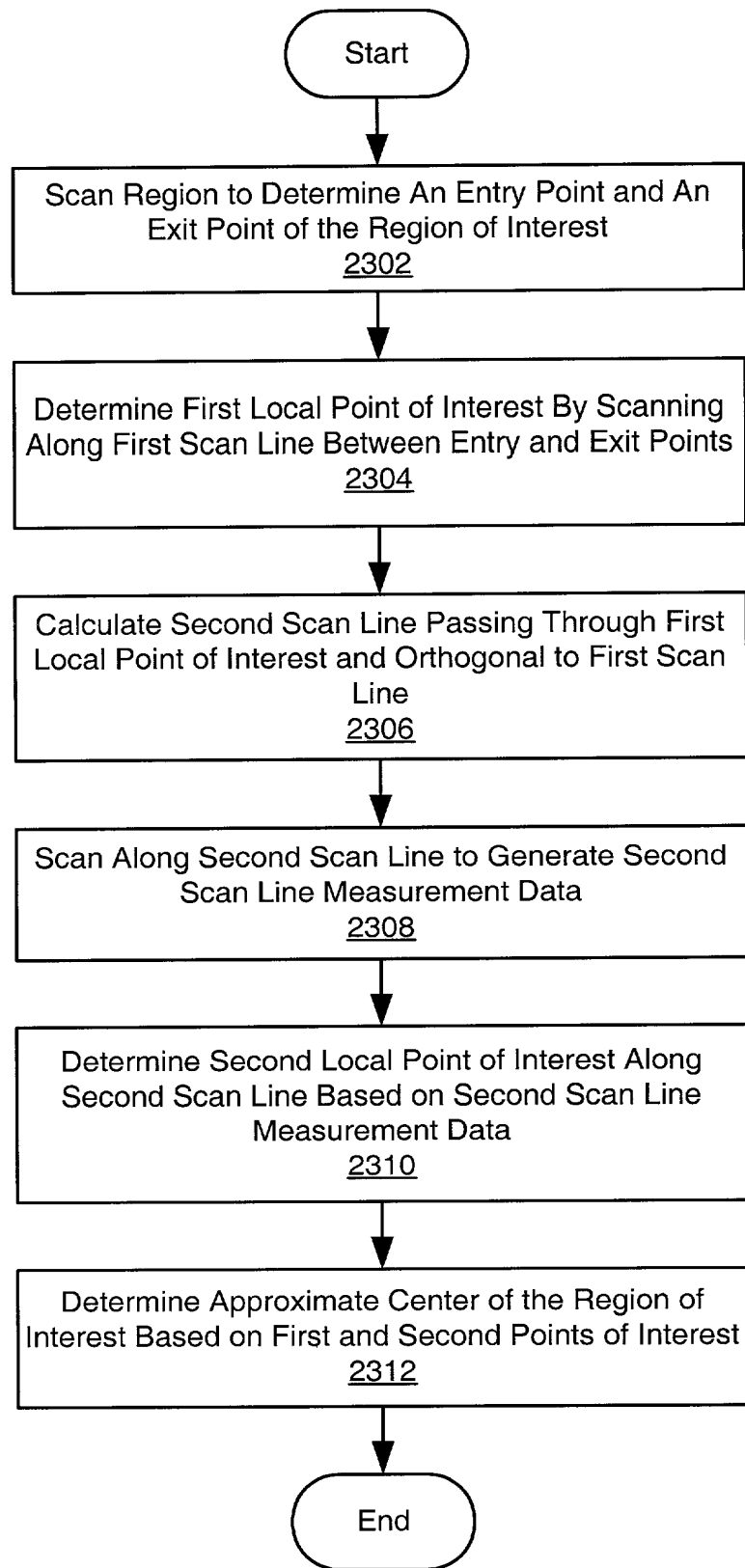


Figure 23